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# **End-to-End Latency Analyzer for ProCom - EELAP**

*Release 0.3.0*

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### Abstract

This report presents an analysis tool *End-to-End Latency Analyzer for ProCom (EELAP)* developed to compute different end-to-end latency semantics for multi-rate components of real-time embedded systems. ProCom component technology implements executable reusable real-time components called *Runnable Virtual Nodes (RVNs)* and supports two different communication strategies for inter-RVN communication. The tool is developed to evaluate the two communication strategies for multi-rate server-based components the ProCom component technology.

In this report we present a user guide for EELAP. We describe the formulas and corresponding algorithms used to compute end-to-end latency semantics, and response-times of the tasks executing in a two-level hierarchical scheduling framework. Further, we provide a detailed description of API's.



# INTRODUCTION

Here we present a brief introduction to the terminologies required to understand the tool. We first explain end-to-end delay analysis and then describe two communication strategies among the ProCom components.

## 1.1 End-to-End Delay Analysis

In embedded systems, the realization of a piece of functionality can follow a flow through many software components. Data may originate at one component (e.g. a sensor) and passes through various other computational components, before terminating at the final component (e.g. an actuator). Hence, the data follows a chain of components ( $C_1, C_2, \dots, C_n$ ), each potentially having its own periodicity and timing properties. The total time taken by the data/signal to traverse the complete chain is called *end-to-end latency* [2]. For an embedded system with real-time constraints, the end-to-end timing behavior is not only dependent on the timing properties of its constituent components but also on the message-chains among those components. In a communication chain, different executable components (or tasks) are activated at different periods. Such system is called a *multi-rate system* [2].

## 1.2 Communication Strategies among ProCom Components

In ProCom component model, the RVNs are implemented as servers (called RVN-server) and the tasks are executed within the servers. This type of systems are called server-based systems or hierarchical systems [3]. The RVN-servers are executed within a two-level hierarchical scheduling implementation [4]. To support communication *between* RVNs (also called *inter-RVN communication*), two different strategies have been proposed [5]. The first strategy is called a *server-based communication*, implemented using a *communication server*. The communication code is embedded within the communication server, which is activated periodically.

Another interesting approach is to use a *direct communication strategy*, where RVNs communicate with each other directly without an intermediate server. Here the communication code is encapsulated within the RVN to send and receive the data and/or messages. The details of both communication strategies for ProCom component model can be found in [5].

Both communication strategies for the ProCom technology reveal the multi-rate systems. According to [2], all automotive embedded systems are multi-rate systems. A system comprising the communication chains among RVN servers transposes to a multi-rate server-based system. Four different end-to-end semantics are provided in [2] for multi-rate systems. We develop the EELAP tool to compute these semantics for multi-rate server-based systems using (1) response times of tasks executed within a server and (2) then end-to-end semantics.

### 1.3 Contributions

We implement a tool *End-to-End Latency Analyzer for ProCom (EELAP)* [6] to evaluate timing behavior of two communication strategies in a multi-rate server-based real-time embedded components using end-to-end latencies (or delays). The tool computes end-to-end latencies using the following two steps:

- First it calculates the response times of all tasks executing in a two-level hierarchical scheduling framework by using methods/formulas provided in [1],
- And then it calculates different end-to-end latency semantics for both communication strategies.

In this report, we present the descriptions of API's of EELAP tool, the formulas and their implementations in those API, and the algorithms for schedulability condition, possible paths, path reachability, and generate paths for different latency semantics.



# USER'S GUIDE

## 2.1 Installation

This tool depends on two external libraries: the [numpy](#) and the [argparse](#). These libraries are not documented here. If you want to dive into their documentation, check out the following links:

- [Numpy Documentation](#)
- [Argparse Documentation](#)

Besides [numpy](#) and [argparse](#), the *lxml* is recommended for full functionality. *pip* or *easy\_install* will install them for you if you do *pip install git+git://github.com/jirikuncar/eelap.git*. We encourage you to use a [virtualenv](#).

## 2.2 Quick start

Eager to get started? This page gives a good introduction how the End-to-End Latency Analysis for ProCom works and how you can benefit from it. It assumes you already have it installed. If you do not, head over to the [Installation](#) section.

### 2.2.1 Finding possible execution paths

The whole simulation is dependant on quick and effective algorithm for finding possible execution paths of tasks in all system components. All latency types are calculated on specified data flow path that contains identifiers of tasks in analyzed system.

Our generator `generate_paths()` returns tuples with activation indexes of tasks accordingly to the analyzed execution path. The algorithm starts with finding closest activation indexes of the first task in path for defined interval. Following pseudo-code shows simplified version of our algorithm using methods `alpha()` and `ialpha()` defined on `Task`.

```
1 function generate_paths(start, stop, tasks_in_path):
2     paths <- list()
3     task <- tasks_in_path.pop(0) # assign and remove first task from the path
4     loop i from task.ialpha(start) to task.ialpha(stop):
```

```
5         # find a time range for next task
6         if length(tasks_in_path) > 0:
7             time <- task.alpha(i)
8             next_task <- tasks_in_path[0] # next task in path
9             j <- next_task.ialpha(time) # closest activation index
10            new_start <- next_tasks.alpha(j) # closest activation time
11            # find possible paths for next task in path from new start.
12            for all path in generate_paths(new_start, stop, tasks_in_path):
13                # join current activation index with found tuple
14                paths.append( path.prepend(i) )
15            end for
16        else:
17            paths.append( list(i) ) # list with only one index
18        end if
19    end loop
20    return paths
21 end function
```

# API REFERENCE

If you are looking for information on a specific function, class or method, this part of the documentation is for you.

## 3.1 API

This part of the documentation covers all the interfaces of End-to-End Analyzer for ProCom.

### 3.1.1 Task

**class** `eelap.Task` (*name, period, priority, exetime*)  
System task.

**C**

Alias for task  $t_i$  execution time ( $C_i$ ).

**HB**

Set of tasks belonging to same Component  $C$  with priorities higher than itself one.

$$HB(s) = \{T_k \in C \mid P(k) > P(s)\}$$

**P**

Alias for task  $t_i$  period ( $P(i)$ ).

**static alpha** ( $i$ )

Calculate time of  $i$ -th activation.

$$\alpha_r(i) = r_{start} + i * P(r)$$

**Parameters**  $i$  – Activation number.

**Returns** Activation time.

**blocking\_time**

Task deadline ( $b_i$ ).

**Warning:** Currently always returns 0.

### **deadline**

Task deadline.

---

**Note:** Currently *deadline==period*.

---

### **static delta (i)**

Calculate response time of *i*-th activation.

**Parameters i** – Activation number.

**Returns** Response time of *i*-th activation.

---

**Note:** In our case we always return task response time.

---

**See Also:**

`response_time()`

### **freq**

Task frequency  $f(t_i) = 1/P(t_i)$ .

### **static ialpha (t)**

Calculate previous activation for given time.

$$\alpha_r^{-1}(t) = \lfloor \frac{t - r_{start}}{P(r)} \rfloor$$

**Parameters t** – Current time.

**Returns** int – activation number.

### **p**

Alias for task  $t_i$  priority ( $p(i)$ ).

### **plan (time)**

Returns True if the task should be scheduled at given *time*.

### **static rbf (t)**

The request bound function.

It computes the maximum cumulative execution requests that could be generated from the time that task is released up to time *t*.

$$rbf_i(t) = C_i + b_i + \sum_{\tau_k \in HP(i)} \frac{t}{T_k} * C_k$$

**Parameters t** – Time limit for execution requests.

**See Also:**

[1] formula (2).

**response\_time**

Task response time.

$$RS(i) = t \mid \exists t : 0 < t \leq D_i, rbf_i(t) \leq sbf_C(t)$$

**status** (*time*)

Returns textual representation of task status at given *time*.

**utilization**

Calculates utilization.

### 3.1.2 Component (Subsystem)

**class** `eelap.Component` (*name, period, priority, budget, scheduler='EDF', pay-back=False*)

System servers / components.

**Bl**

The maximum blocking imposed to a this subsystem.

$$Bl(s) = \max\{X(k) \mid S_k \in LPS(s)\}$$

**See Also:**

[1] formula (10).

**HPS**

Set of subsystems of `System S` with priority higher than itself ( $S_s$ ).

$$HSP(s) = \{S_k \in S \mid P(k) > P(s)\}$$

**See Also:**

Used in formula (9) in [1].

**LPS**

Set of subsystems of `System S` with priority lower than itself ( $S_s$ ).

$$LSP(s) = \{S_k \in S \mid P(k) < P(s)\}$$

**See Also:**

Used in formula (10) in [1].

**P**

Alias for `Component` period.

**Q**

Alias for `Component` budget.

### **RBF** (*t*)

Request Bound Function

#### **See Also:**

[1] formula (9) and (11).

### **x**

The maximum execution-time that any subsystem-internal task may lock a shared global resource.

**Warning:** Currently always returns 0.

### **deadline**

The function returns `Component` deadline.

Currently the `self.deadline==self.period`.

### **f1** (*t*)

Implementation of helper formula *f1*.

**Parameters** *t* – time

#### **See Also:**

[1] formula (5).

### **f2** (*t*)

Implementation of helper formula *f2*.

**Parameters** *t* – time

#### **See Also:**

[1] formula (6).

### **freq**

The function calculates `Component` frequency.

### **static sbf** (*t*)

Supply Bound Function.

If `payback` is `True` then this method depends on `f1()` and `f2()`:

```
return max(min(f1(t), f2(t)), 0)
```

**Parameters** *t* – time

#### **See Also:**

[1] formula (3) and (4).

### **schedulability**

`Component` schedulability condition.

```

for t in C_{tasks}:
  schedulable <- False
  for i in [1..P(t)]:
    if rbf_t(i) <= sbf_C(i):
      schedulable <- True
      break
    end if
  end for
  if not schedulable:
    return False
  end if
end for
return True

```

**See Also:**

[1] formula (13).

**utilization**

Returns `Component` utilization as product of its frequency and budget.

### 3.1.3 System

**class** `eelap.System` (*scheduler='FPS', resolution=1000, components=None*)

Models a physical system with instances of `Component`.

**B** (*t*)

Blocking time left at given *time*.

**Warning:** Currently always returns 0.

**static TP\_first** (*possible\_paths*)

Set of all non-duplicate, reachable timed paths, for which no timed path exists that shares the same start instance of the first task and has an earlier end instance of the last task.

$$\mathbb{TP}^{first} = \{\vec{tp} \in \mathbb{TP}^{reach} \mid \neg \exists \vec{tp}' \in \mathbb{TP}^{reach} : tp'_1 = tp_1 \wedge tp'_n < tp_n\}$$

```

function earlier(tp, tp'):
  # index -1 gets last element in array
  return tp'[0] == tp[0] and tp'[-1] < tp[-1]
end function

```

```

out <- list()
TP_reach_paths <- TP_reach(possible_paths)
for tp in TP_reach_paths:
  if not any(map(partial(earlier, tp), TP_reach_paths)):
    out.append(tp)

```

```

        end if
    end for
return out

```

**See Also:**

[2] formula (11).

**static TP\_reach** (*possible\_paths*)

It obtains the set of all paths and returns only all reachable timed path ( $\mathbb{TP}^{reach}$ ).

```

out <- list()
for all path in possible_paths:
    if reach_path(path):
        out.append(path)
    end if
end for
return out

```

**See Also:**

[2] formula (9).

**addComponent** (*component*)

Adds new `Component` instance to the system.

It stores reference of the system to added component.

**Parameters** `component` (`Component`) – New system subsystem.

**static att** (*w, i, r, j*)

It returns *True* if “activation time travel” occurs ( $att(t_w(i) \rightarrow t_r(j))$ ).

The activation time travel occurs when the reader is activated before the writer ( $\alpha_r(i)$  is equivalent to `alpha()` on `t()`).

$$att(t_w(i) \rightarrow t_r(j)) = \alpha_r(j) < \alpha_w(i)$$

**Parameters**

- **w** – Index of writer task in data path.
- **i** – Activation index of writer task.
- **r** – Index of reader task in data path.
- **j** – Activation index of reader task.

**See Also:**

[2] formula (3)

**static crit** (*w, i, r, j*)

The “critical function” determines if writer and reader overlap in execution even in



case of non-activation time travel ( $crit(t_w(i) \rightarrow t_r(j))$ ).

$$crit(t_w(i) \rightarrow t_r(j)) = \alpha_r(j) < \alpha_w(i) + \delta_w(i)$$

### Parameters

- **w** – Index of writer task in data path.
- **i** – Activation index of writer task.
- **r** – Index of reader task in data path.
- **j** – Activation index of reader task.

### See Also:

[2] formula (4)

**delta\_FF** (*ls*)

Find maximum of First-to-First path delays.

### See Also:

[2] formula (17).

**delta\_FF\_path** (*path, tp\_reach*)

Calculate First-to-First path delay.

$$\Delta^{FF}(\vec{tp}) = \Delta^{LF}(\vec{tp}) + \alpha_1(tp_1) - \alpha_1(pred(\vec{tp}))$$

### Parameters

- **path** – Array with task activation numbers.
- **tp\_reach** – List of reachable paths.

**Fixme** remove dependency on *tp\_reach* parameter.

### See Also:

[2] formula (16).

**delta\_FL** (*ls*)

Find maximum of First-to-Last path delays.

### See Also:

[2] formula (15).

**delta\_FL\_path** (*path, tp\_reach*)

Calculate First-to-Last path delay (uses `pred()`).

$$\Delta^{FL}(\vec{tp}) = \Delta^{LL}(\vec{tp}) + \alpha_1(tp_1) - \alpha_1(pred(\vec{tp}))$$

### Parameters

- **path** – Array with task activation numbers.
- **tp\_reach** – List of reachable paths.

**Fixme** remove dependency on *tp\_reach* parameter.

**See Also:**

[2] formula (14).

**static delta\_LF** (*ls*)

The maximum “Last-to-First” timed path delay.

$$\Delta^{LF}(p) = \max\{\Delta(\vec{tp}) \mid \vec{tp} \in \mathbb{TP}^{first}\}$$

**See Also:**

[2] formula (12).

**static delta\_LL** (*possible\_paths*)

Returns maximum latency over all reachable paths (`TP_reach()`).

$$\Delta^{LL}(\text{possible\_paths}) = \max\{\Delta(\text{path}) \mid \text{path} \in \mathbb{TP}^{reach}\}$$

```
# map .. calls function for each element in list
# max .. returns maximal element from list
return max(map(delta_path, TP_reach(possible_paths)))
```

**See Also:**

[2] formula (10).

**delta\_LL\_path** (*path*)

Calculate Last-to-Last *path* delay using `delta_path()`.

**delta\_path** (*path*)

Calculate end-to-end *path* delay.

$$\Delta(\text{path}) = \alpha_n(\text{path}_n) + \delta_n(\text{path}_n) - \alpha_1(\text{path}_1)$$

**See Also:**

[2] formula (2).

**static forw** (*w, i, r, j*)

It determines the forward reachability of the two task instances  $t_w$  and  $t_r$ .

$$\text{forw}(t_w(i) \rightarrow t_r(j)) = \neg \text{att}(t_w(i) \rightarrow t_r(j)) \wedge (\neg \text{crit}(t_w(i) \rightarrow t_r(j)) \vee \text{wait}(t_w(i) \rightarrow t_r(j)))$$

**Parameters**

- **w** – Index of writer task in data path.
- **i** – Activation index of writer task.
- **r** – Index of reader task in data path.
- **j** – Activation index of reader task.

**See Also:**

[2] formula (6)

**generate\_paths** (*index, start, stop*)

Generator of possible paths for given task in path.

It yields tuples with task activation index starting from ‘index’th task in defined path.

```
paths <- list()
task <- tasks_in_path.pop(0) # assign and remove first task from the pa
loop i from task.ialpha(start) to task.ialpha(stop):
    # find a time range for next task
    if length(tasks_in_path) > 0:
        time <- task.alpha(i)
        next_task <- tasks_in_path[0] # next task in path
        j <- next_task.ialpha(time) # closest activation index
        new_start <- next_tasks.alpha(j) # closest activation time
        # find possible paths for next task in path from new start.
        for all path in generate_paths(new_start, stop, tasks_in_path):
            # join current activation index with found tuple
            paths.append( path.prepend(i) )
        end for
    else:
        paths.append( list(i) ) # list with only one index
    end if
end loop
return paths
```

**pred** (*path, tp\_reach*)

Temporal distance to the start of the latest previous “last-to-x” path.

**See Also:**

[2] formula (13).

**static reach** (*w, i, r, j*)

The output of an instance  $t_w(i)$  is overwritten by instance  $t_w(i + 1)$  when both instances can forward reach the same reading task instance  $t_r(j)$ . In other words,  $t_w(i)$  can reach  $t_r(j)$  if and only if the following function returns *True*:

$$reach(t_w(i) \rightarrow t_r(j)) = (forw(t_w(i) \rightarrow t_r(j)) \wedge \neg forw(t_w(i + 1) \rightarrow t_r(j)))$$

**Parameters**

- **w** – Index of writer task in data path.

- **i** – Activation index of writer task.
- **r** – Index of reader task in data path.
- **j** – Activation index of reader task.

**See Also:**

[2] formula (7).

**static reach\_path** (*path*)

Check *path* reachability.

```
path_length <- length(path)
for i in [0..path_length-1]:
  tp_i <- path[i]
  tp_i1 <- path[i+1]
  if reach(t_w(tp_i) -> t_{w+1}(tp_i1)):
    return False
  end if
end for
return True
```

**See Also:**

[2] formula (8).

**schedulability**

This method checks the global schedulability condition.

```
for C in components:
  # P(C) .. period of component C
  schedulable <- False
  for t in [0..P(C)]:
    if RBF(C, t) <= t:
      schedulable <- True
      break
    end if
  end for
  if not schedulable:
    return False
  end if
end for
return True
```

**See Also:**

[1] formula (8).

**t** (*i*)

Get *i*-th `Task` instance ( $t_i$ ).

**Parameters** **i** – The index of system task starting from 0.

**Returns** Instance of `Task`.

**tasks**

All system tasks.

**tasks\_in\_path**

List of tasks in data path.

**utilization**

Returns system utilization calculated as sum of component utilizations.

**static wait** (*w, i, r, j*)

It determines if the writer finishes first, because the reader has to wait due to its priority in case of overlapped but not time-traveling execution ( $wait(t_w(i) \rightarrow t_r(j))$ ).

$$wait(t_w(i) \rightarrow t_r(j)) = p(t_r) < p(t_w)$$

**Parameters**

- **w** – Index of writer task in data path.
- **i** – Activation index of writer task.
- **r** – Index of reader task in data path.
- **j** – Activation index of reader task.

**See Also:**

[2] formula (5)



## ADDITIONAL NOTES

Design notes, legal information and changelog are here for the interested.

### 4.1 Licence

Source code is distributed under following GNU/GPLv2 licence.

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